



Common Vertical Force and Bending Moment Diagrams

| Beam Type                           | Simple   | Simple  | Simple   | Simple                                    | Simple  | Fixed at Both Ends   | Fixed at Both Ends   | Cantilever  | Cantilever   |
|-------------------------------------|--|---|--|---|---|--|--|---|--|
| Free Body Diagram                   |  |   |  |   |   |  |  |   |  |
| Vertical Force (V) or Shear Diagram |  |   |  |   |   |  |  |   |  |
| Bending Moment (M) Diagram          |  |   |  |   |   |  |  |   |  |
| Load                                | Concentrated Load at Centre                    | Concentrated Load at Any Point                  | 2 Unequal Concentrated Loads Unsymmetrically Placed                              | Uniformly Distributed Load                | Load Increasing Uniformly Towards One End                               | Concentrated Load at any Point   | Uniformly Distributed Loads  | Concentrated Load at any Point  | Uniformly Distributed Loads  |
| Connectors                          | Pin and Roller                                 | Pin and Roller                                  | Pin and Roller   | Pin and Roller                            | Pin and Roller  | Fixed  | Fixed  | Cantilever  | Cantilever   |
| Reactions                           | $R = V$  | $R_1 = V_1$<br>$R_2 = V_2$                      | $R_1 = V_1$<br>$R_2 = V_2$   | $R = V$                                   | $R_1 = V_1$<br>$R_2 = V_2$  | $R_1 = V_1$<br>$R_2 = V_2$   | $R = V$  | $R = V$   | $R = V$  |
| Vertical Force                      | $V = \frac{P}{2}$                              | $V_1 = \frac{Pb}{l}$<br>$V_2 = \frac{Pa}{l}$    | $V_1 = \frac{P_1(l-a) + P_2b}{l}$<br>$V_2 = \frac{P_2(l-b) + P_1a}{l}$           | $V = \frac{wl}{2}$                        | $V_1 = \frac{W}{3}$<br>$V_2 = \frac{2W}{3}$<br>where $W = \frac{wl}{2}$ | $V_1 = \frac{Pb^2(3a+b)}{l^3}$<br>$V_2 = \frac{Pa^2(3b+a)}{l^3}$   | $V = \frac{wl}{2}$   | $V = P$   | $V = wl$<br>$V_x = wx$   |
| Bending Moment                      | $M_{max} = \frac{Pl}{4}$<br>(at point of load) | $M_{max} = \frac{Pab}{l}$<br>(at point of load) | $M_1 = R_1a$<br>(max. if $R_1 > P_1$ )<br>$M_2 = R_2b$<br>(max. if $R_2 > P_2$ ) | $M_{max} = \frac{wl^2}{8}$<br>(at centre) | $M_{max} = \frac{2Wl}{9\sqrt{3}}$<br>$= .1283Wl$                        | $M_1 = \frac{Pab^2}{l^2}$<br>(max. if $a < b$ )<br>$M_2 = \frac{Pba^2}{l^2}$<br>(max. if $a > b$ )<br>$M_a = \frac{2Pb^2a^2}{l^3}$<br>(at point of load) | $M_{max} = \frac{wl^2}{12}$<br>(at ends)<br>$M_1 = \frac{wl^2}{24}$<br>(at centre) | $M_{max} = Pb$<br>(at fixed end)<br>$M_x = P(x-a)$<br>(when $x > a$ ) | $M_{max} = \frac{wl^2}{2}$<br>(at fixed end)<br>$M_x = \frac{wx^2}{2}$ |